## MORE WORK FACTORING TRINOMIALS COMMON CORE ALGEBRA I

Factoring trinomials, which we first practiced in the last lesson, is a trying experience. All algebra students must learn how to do this procedure because of its immense number of **practical applications**. We will eventually see these applications, but for now, we need to get more practice factoring these trinomials. We begin by looking at a process known as **complete factoring**.

*Exercise* #1: Consider the trinomial  $4x^2 + 20x + 24$ .

- (a) Write this trinomial as an equivalent expression involving the product of its term's gcf and another trinomial.
- (b) Factor this additional trinomial to express the original in **completely factored form**.

Whenever we factor, we should always look to see if a greatest common factor exists that can be "factored out" to begin the problem. This will always make any subsequent factoring easier.

*Exercise* #2: Rewrite each of the following trinomials in completely factored form.

(a)  $10x^2 + 15x - 10$  (b)  $3x^3 - 21x^2 + 36x$ 

(c)  $7x^2 + 21x - 70$ 

(d)  $6x^2 - 2x - 4$ 





Complete factoring can also involve factoring the **difference of perfect squares**. Try the next exercise to see how this works.

*Exercise* #3: Write each of the following binomials in completely factored form.

(a)  $2x^2 - 18$  (b)  $5x^3 - 20x$ 

(c)  $12x^2 - 3$  (d)  $54x^2 - 24$ 

If you understand factoring as breaking an expression into an equivalent product, then essentially you can always check to see if you have factored correctly. Complete factoring actually leads to a nice way to eliminate some guesses from trinomial guess and check methods.

*Exercise* #4: Consider the trinomial  $2x^2 + 11x + 12$ .

- (a) Do the three terms of this trinomial have a gcf other than 1?
- (b) Why would the guesses (2x+2)(x+6), (2x+4)(x+3), and (2x+12)(x+1) not make sense given your answer to (a)?

- (c) Fill in the statement:
  - If a trinomial does not have a gcf, then

\_\_\_\_\_ of its \_\_\_\_\_ factors will

(d) Factor this trinomial by limiting your guesses.

have a gcf.

*Exercise* #5: Use the Smart Guessing Tip from the last problem to factor  $4x^2 - 21x - 18$ .





## MORE WORK FACTORING TRINOMIALS COMMON CORE ALGEBRA I HOMEWORK

## FLUENCY

- 1. Rewrite each of the following trinomials in completely factored form.
  - (a)  $2x^2 + 20x + 42$  (b)  $6x^2 + 33x + 15$

(c) 
$$5x^2 - 10x - 40$$
 (d)  $30x^2 + 20x - 10$ 

(e) 
$$x^3 + 7x^2 + 10x$$
 (f)  $4x^3 + 10x^2 - 24x$ 

(g) 
$$5x^2 - 45$$
 (h)  $2x^3 - 2x$ 

(i)  $36-4x^2$  (j)  $20x^2-125$ 

- 2. Which of the following is *not* a factor of  $4x^3 + 12x^2 72x$ ? Show work that justifies your choice.
  - (1) (x+9) (3) (x-3)
  - (2) 4x (4) (x+6)





- 3. Which of the following is the missing factor in the product 2(x-1)(?) if it is equivalent to the trinomial  $2x^2 + 10x 12?$ 
  - (1) x+12 (3) x+3
  - (2) x+6 (4) x-5
- 4. Use the Smart Guessing Tip from Exercise #4 to help factor the following challenging trinomials. Note that they do **not** have a greatest common factor.
  - (a)  $4x^2 + 19x + 12$  (b)  $6x^2 + 7x 24$

## REASONING

- 5. Consider the **cubic trinomial**  $x^3 + 8x^2 + 7x$ .
  - (a) Write this trinomial as an equivalent product in completely factored form.
- (b) How can the original trinomial and your answer to (b) help you determine the value of (10)(17)(11) without a calculator? What is the value?

6. Use the complete factorization of  $2x^3 + 8x^2 + 8x$  to determine the value of the product  $(20)(12)^2$ . Explain your reasoning.



