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## GRAPHS OF LINEAR INEQUALITIES Common Core Algebra I



So, we have graphed linear functions and in the last lesson learned that the points that lie on a graph are simply the $(x, y)$ pairs that make the equation true. Graphing an inequality in the $x y$-plane is exactly the same

## Graphing InEQUALITIES

To graph an inequality simply means to plot (or shade) all $(x, y)$ pairs that make the inequality true

Exercise \#1: Consider the inequality $y>x+3$.
(a) Determine whether each of the following points lies in the solution set (and thus on the graph of) the inequality given.

$$
\begin{equation*}
(2,7) \tag{0,1}
\end{equation*}
$$

(b) Graph the line $y=x+3$ on the grid below in dashed form. Why are points that lie on this line not part of the solution set of the inequality?

(c) Plot the three points from part (a) and use them to help you shade the proper region of the plane that represents the solution set of the inequality.
(d) Choose a fourth point that lies in the region you shaded and show that it is in the solution set of the inequality.
(e) The point $(10,12)$ cannot be drawn on the graph grid above, so it is difficult to tell if it falls in the shaded region. Is $(10,12)$ part of the solution set of this inequality? Show how you arrive at your answer.

There are some challenges to graphing linear inequalities, especially if the output, $y$, has not been solved for. Let's look at the worst case scenario.

Exercise \#2: Consider the inequality $3 x-2 y \geq 2$
(a) Rearrange the left-hand side of this inequality using the commutative property of addition.
(b) Solve this inequality for $y$ by applying the properties of inequality that we used in Unit \#2.
(c) Shade the solution set of this inequality on the graph paper below.

(d) Pick a point in the shaded region and show that it is a solution to the original inequality.

The final type of inequality that we should be able to graph quickly and effectively is one that involves either a horizontal line or a vertical line.

Exercise \#3: Shade the solution set for each of the following inequalities in the xy-planes provided. First, state in your own words the $(x, y)$ pairs that the inequality is describing.
(a) $x<4$

Your own words:
(b) $y \geq-2$

Your own words:


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## GRAPHS OF LINEAR INEQUALITIES Common Core Algebra I Homework

## FLUENCY

1. Determine which of following points lie in the solution set of the inequality $y \geq 2 x-4$ and which do not. Justify each choice.
(a) $(5,4)$
(b) $(0,-1)$
(c) $(10,16)$
(d) $(2,-1)$
2. Which of the following points lies in the solution set of the inequality $y \geq 3 x+10$ ?
(1) $(1,10)$
(3) $(4,20)$
(2) $(-1,3)$
(4) $(2,16)$
3. Which of the following points does not lie in the solution set to the inequality $y \geq-\frac{1}{3} x+5$ ?
(1) $(6,3)$
(3) $(-3,8)$
(2) $(-6,5)$
(4) $(12,3)$
4. Which of the following linear inequalities is shown graphed below?
(1) $y<\frac{3}{2} x-1$
(3) $y>\frac{2}{3} x-1$
(2) $y \leq \frac{2}{3} x-1$
(4) $y \geq \frac{3}{2} x-1$

5. Graph the solution set to the inequality shown below. State one point that lies in the solution set and one point that does not.
$y<-2 x+4$

One Point In Solution: One Point Not In Solution:

6. Rearrange the inequality below so that it is easier to graph and then sketch its solution set on the grid given. Be careful when dividing by a negative and remember to switch the inequality sign.

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x-2 y \leq 6
$$

One Point In Solution: One Point Not In Solution:

7. Graph the solution set to each of the following inequalities.
(a) $y \leq 4$

(b) $x>1$


